

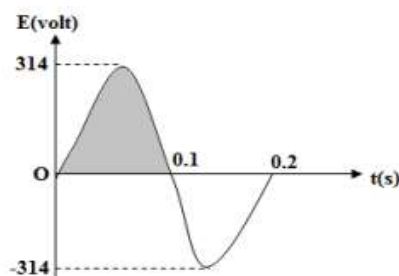
Board -

Class - 12

Topic - Alternating Current

## LEVEL-I

1. What is the self-inductance of a coil in which magnetic flux of  $40\text{mWb}$  is produced when  $2\text{A}$  current flow through it?
2. If the self-inductance of an air core inductor increases from  $0.01\text{mH}$  to  $100\text{mH}$  on introducing an iron core into it. What is relative permeability of the core used?
3. What is the power dissipated in an ac circuit in which voltage and current are given by  $V = 230 \sin(\omega t + \pi/2)$  and  $i = 10 \sin \omega t$  ?
4. When a lamp is connected to an ac supply it lights with the same brightness as when connected to a  $12\text{V}$  dc battery. What is the peak value of alternating voltage?
5. Find the capacitance of the capacitor that would have reactance of  $100\Omega$  when used with ac source of frequency  $\frac{5}{\pi}\text{kHz}$ ?
6. What is the average value of the emf for the shaded part of graph?



7. In a series LCR circuit the voltage across an inductor, a capacitor and a resistor are  $20\text{V}$ ,  $20\text{V}$  and  $60\text{V}$  respectively. What is the phase difference between the applied voltage and the current in the circuit?
8. A circular coil of radius  $8\text{ cm}$  and  $20$  turns rotates about its vertical diameter with an angular speed of  $50$  revolutions per second in a uniform horizontal magnetic field of magnitude  $3 \times 10^{-2}\text{ T}$ . Find the maximum and average value of the emf induced in the coil.
9. The instantaneous current from an ac source is  $i = 5 \sin (314 t)$  ampere. What are the average and rms values of the current?

10. An inductor  $L$ , a capacitor  $20\ \mu\text{F}$ , a resistance  $10\ \Omega$  are connected in series with an ac source of frequency  $50\text{Hz}$ . If the current is in phase with voltage, calculate the Inductance  $L$ .

### LEVEL-II

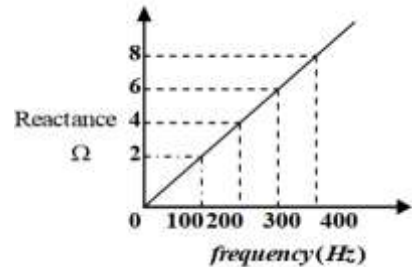
1. A conductor of length  $1.0\ \text{m}$  falls freely under gravity from a height of  $10\ \text{m}$  so that it cuts the lines of force of the horizontal component of earth's magnetic field of  $3 \times 10^{-5}\ \text{T}$ . Find the emf induced in the conductor.
2. A  $0.4\ \text{m}$  long straight conductor is moved in a magnetic field of induction  $0.9\ \text{Wbm}^{-2}$  with velocity of  $7\ \text{ms}^{-1}$ . Calculate the maximum emf induced in the conductor.
3. A metal disc of radius  $200\ \text{cm}$  is rotated at a constant angular speed of  $60\ \text{rad/s}$  in a plane at right angles to an external field of magnetic induction  $0.05\ \text{Wbm}^{-2}$ . Find the emf induced between the centre and a point on the rim.
4. Find the maximum value of current when an inductance of one Henry is connected to an ac source of  $200\ \text{volts}$ ,  $50\ \text{Hz}$ .
5. What is the inductive reactance of a coil if current through it is  $800\ \text{mA}$  and the voltage across it is  $40\ \text{V}$ ?
6. A transformer has  $300$  primary turns and  $2400$  secondary turns. If the primary supply voltage is  $230\ \text{V}$ , what is the secondary voltage?
7. A transformer of  $100\%$  efficiency has  $500$  turns in the primary and  $10,000$  turns in the secondary coil. If the primary is connected to  $220\ \text{V}$  supply, what is the voltage across the secondary coil?
8. A capacitor in series with a resistance of  $30\ \text{ohm}$  is connected to a.c. mains. The reactance of the capacitor is  $40\ \Omega$ . Calculate the phase difference between the current and the supply voltage.
9. Determine the impedance of a series LCR-circuit if the reactance of  $C$  and  $L$  are  $250\ \Omega$  and  $220\ \Omega$  respectively and  $R$  is  $40\ \Omega$ .
10. A series circuit with  $L=0.12\ \text{H}$ ,  $C=0.48\ \text{mF}$  and  $R=25\ \Omega$  is connected to a  $220\ \text{V}$  variable frequency power supply. At what frequency is the circuit current maximum?

### LEVEL-III

1. A bulb of resistance  $10\Omega$ , connected to an inductor of inductance  $L$ , is in series with an ac source marked  $100\text{V}$ ,  $50\text{Hz}$ . If the phase angle between the voltage and current is  $\frac{\pi}{4}$  radian, calculate the value of  $L$ .

2. Figure shows how the reactance of an inductor varies with frequency.

- a) Calculate the value of inductance of the inductor using the information given in the graph.  
b) If this inductor is connected in series to a resistor of  $8\ \text{ohm}$ , find what would be the impedance at  $300\ \text{Hz}$



3. In a series RC circuit,  $R = 30\Omega$ ,  $C = 0.25\ \mu\text{F}$ ,  $V = 100\ \text{V}$  and  $\omega = 10,000$  radian per second. Find the current in the circuit and calculate the voltage across the resistor and the capacitor. Is the algebraic sum of these voltages more than the source voltage? If yes, resolve the paradox.
4. When an alternating voltage of  $220\text{V}$  is applied across a device  $X$ , a current of  $0.5\text{A}$  flows through the circuit and in phase with the applied voltage. When the same voltage is applied across another device  $Y$ , the same current again flows through the circuit but it leads the applied voltage by  $\pi/2$  radians.
- a) Name the devices  $X$  and  $Y$   
b) Calculate the current flowing in the circuit when the same voltage is applied across the series combination of  $X$  and  $Y$ .
5. In the series LCR circuit, suppose  $R = 300\ \Omega$ ,  $L = 60\ \text{mH}$ ,  $C = 0.5\ \mu\text{F}$ . An ac source of emf  $50\ \text{V}$ , angular frequency  $10,000\ \text{rad/s}$  is connected across the combination. Find the reactance  $X_L$ , and  $X_C$ , the impedance  $Z$ , the current amplitude  $I$ , the phase angle  $\phi$ , and the voltage amplitude across each circuit element.
6. In a series RC circuit with an AC source,  $R = 300\Omega$ ,  $C = 25\ \mu\text{F}$ ,  $E_0 = 50\ \text{V}$  and  $\omega = \frac{50}{\pi}$ , find the peak current and the average power dissipated in the circuit.
7. An inductor  $200\ \text{mH}$ , capacitor  $500\ \mu\text{F}$ , resistor  $10\ \Omega$  are connected in series with a  $100\ \text{V}$ , variable frequency ac source. Calculate the
- a) frequency at which the power factor of the circuit is unity  
b) current amplitude at this frequency  
c) Q-factor
8. A resistor of resistance  $400\Omega$ , and a capacitor of reactance  $200\mu\text{F}$ , are connected in series to a  $220\ \text{V}$ ,  $50\ \text{Hz}$  ac source. If the current in the circuit is  $0.49\ \text{A}$ , find
- a) voltage across the resistor and capacitor  
b) value of inductance required so that voltage and current are in phase.

9. A resistor of  $200\Omega$  and a capacitor of  $15\ \mu\text{F}$  are connected in series to a  $220\ \text{V}$ ,  $50\ \text{Hz}$  ac source.
- Calculate the current in the circuit
  - Calculate the voltage (rms) across the resistor and the capacitor. Is the algebraic sum of these voltages more than the source voltage? If yes, resolve the paradox.
10. A town is situated  $15\ \text{km}$  away from a power plant generating power at  $440\text{V}$ , requires  $800\ \text{kW}$  of electric power at  $220\text{V}$ . The resistance of the two wire line carrying power is  $0.5\ \text{ohm per km}$ . The town gets power from the line through a  $4000\text{-}220\text{V}$  step down transformer at a substation in the town.
- Find the line power losses in the form of heat.
  - How much power must the plant supply, assuming there is negligible power loss due to leakage?
  - Characterize the step up transformer at the plant.
11. An ac generator consists of a coil of  $50$  turns and area  $2.5\ \text{m}^2$  rotating at an angular speed of  $60\ \text{rad/s}$  in a uniform magnetic field  $B = 0.3\ \text{T}$  between two fixed pole pieces. The resistance of the circuit including that of the coil is  $500\ \Omega$ . Determine the Calculate
- Maximum current drawn from the generator
  - Maximum power dissipation in the coil
  - What will be orientation of the coil with respect to the magnetic field to have (a) maximum, (b) zero magnetic flux?
  - Would the generator work if the coil was stationary and instead the pole pieces rotated together with the same speed as above?
12. A circular coil having  $20$  turns, each of radius  $8\ \text{cm}$ , is rotating about its vertical diameter with an angular speed of  $50\ \text{rad/s}$  in a uniform horizontal magnetic field of magnitude  $30\ \text{mT}$ . Obtain the maximum average and rms value of the emf induced in the coil. If the coil forms a closed loop of resistance  $10\ \Omega$ , how much power is dissipated as heat in it?
13. An athlete peddles a stationary tricycle whose pedals are attached to a coil having  $100$  turns each of area  $0.1\ \text{m}^2$ . The coil, lying in the  $X - Y$  plane, is rotated, in this plane, at the rate of  $50\ \text{rpm}$ , about the  $Y$ -axis, in a region where a uniform magnetic field,  $\mathbf{B} = 0.01\ \hat{k}$  Tesla, is present. Find the
- maximum emf
  - average e.m.f generated in the coil over one complete revolution

### Answers of Level I

1. 20 mH.                      2. 1000                      3. zero                      4. 16.92V                      5.  $10^6 F$                       6. 200V  
7. 0 rad.                      8.  $\varepsilon_{max} = 0.6 V$ ;  $\varepsilon_{av} = 0 V$                       9. average value of current = 0, rms value of current =  $\frac{5}{\sqrt{2}} A$   
10.  $2 \times 10^5 H$ ]

### Answers of Level II

- Q1:-  $4.2 \times 10^{-4} V$  , Q2:- 2.52 V , Q3:- 6 V , Q4:- 0.9 A , Q5:- 50 ohm , Q6:- 1.84 kV , Q7:- 4400 V , Q8:-  $\tan^{-1} 4/3$  , Q9:- 50 ohm , Q10:- 21 Hz

### Answers of Level III

$$\text{Ans1. } \cos \phi = \frac{R}{Z} \quad \Rightarrow \cos \frac{\pi}{4} = \frac{R}{\sqrt{R^2 + X_L^2}} \quad \Rightarrow X_L = R \quad \Rightarrow L = 3.14 \times 10^{-2} H$$

$$\text{Ans2. (a) } L = \frac{X_L}{2\pi\nu} \quad (\text{b) at } 300 \text{ Hz; } X_L = 6 \Omega, R = 8 \Omega \quad \Rightarrow Z = \sqrt{R^2 + X_L^2} = 10 \Omega$$

$$\text{Ans3. } X_C = \frac{1}{2\pi\nu C} = 400 \Omega; \quad Z = \sqrt{R^2 + X_C^2} = 500 \Omega; \quad i = \frac{e}{Z} = \frac{100}{500} = 0.2 A$$

rms voltage drop on R =  $V_R = i_{rms} R = 60 V$ ; rms voltage drop on C =  $V_C = i_{rms} X_C = 80 V$