



CBSE 10th

TEEVRA EDUTECH PVT. LTD.

Q.1 Draw a line segment of length 7.6 cm and divide it in the ratio 5:8. Measure the two parts.
Give the justification of the construction.

Sol: A line segment of length 7.6 cm can be divided in the ratio of 5:8 as follows.

Step 1 Draw line segment AB of 7.6 cm and draw a ray AX making an acute angle with line segment AB.

Step 2 Locate 13 (= 5 + 8) points, $A_1, A_2, A_3, A_4, \dots, A_{13}$, on AX such that $AA_1 = A_1A_2 = A_2A_3$ and so on.

Step 3 Join BA_{13} .

Step 4 Through the point A_5 , draw a line parallel to BA_{13} (by making an angle equal to $\angle AA_{13}B$) at A_5 intersecting AB at point C.

C is the point dividing line segment AB of 7.6 cm in the required ratio of 5 : 8.

The lengths of AC and CB can be measured. It comes out to 2.9 cm and 4.7 cm respectively.

Justification : The construction can be justified

by proving that

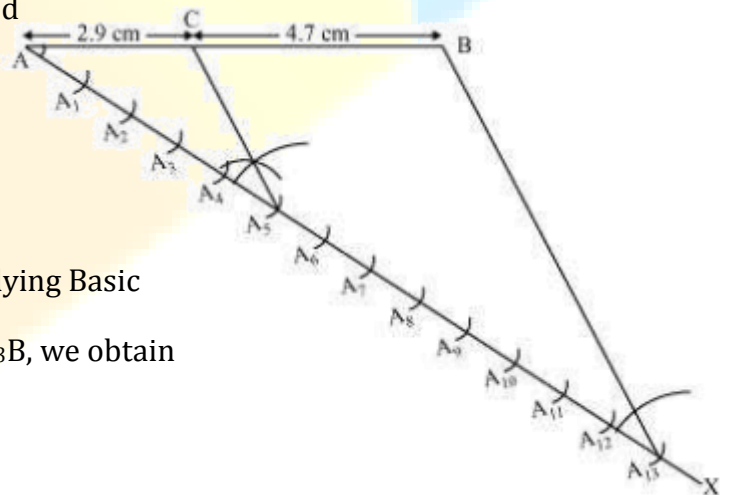
$$\frac{AC}{CB} = \frac{5}{8}$$

By construction, we have $A_5C \parallel A_{13}B$. By applying Basic

proportionality theorem for the triangle $AA_{13}B$, we obtain

$$\frac{AC}{CB} = \frac{AA_5}{A_5A_{13}} \quad \dots (1)$$

From the figure, it can be observed that AA_5 and A_5A_{13} contain 5 and 8 equal divisions of line segments respectively.



$$\therefore \frac{AA_5}{A_5A_{13}} = \frac{5}{8} \quad \dots (1)$$

On comparing equations (1) and (2), we obtain

$$\frac{AC}{CB} = \frac{5}{8}$$

This justifies the construction.

Q.2 Construct a triangle of sides 4 cm, 5cm and 6cm and then a triangle similar to it whose sides are $\frac{2}{3}$ of the corresponding sides of the first triangle. Give the justification of the construction.

Sol: **Step 1**

Draw a line segment $AB = 4$ cm. Taking point A as centre, draw an arc of 5 cm radius. Similarly, taking point B as its centre, draw an arc of 6 cm radius. These arcs will intersect each other at point C.

Now, $AC = 5$ cm and $BC = 6$ cm and ΔABC is the required triangle.

Step 2

Draw a ray AX making an acute angle with line AB on the opposite side of vertex C.

Step 3

Locate 3 points A_1, A_2, A_3 (as 3 is greater between 2 and 3) on line AX

such that $AA_1 = A_1A_2 = A_2A_3$.

Step 4

Join BA_3 and draw a line through A_2 parallel to BA_3 to intersect AB at point B' .

Step 5

Draw a line through B' parallel to the line BC to intersect AC at C' .

$\Delta AB'C'$ is the required triangle.

Justification

The construction can be justified by proving that

$$AB' = \frac{2}{3} AB, B'C' = \frac{2}{3} BC, AC' = \frac{2}{3} AC$$

By construction, we have $B'C' \parallel BC$

$$\therefore \angle A B' C' = \angle ABC \text{ (Corresponding angles)}$$

In $\triangle AB'C'$ and $\triangle ABC$,

$$\angle AB'C' = \angle ABC \text{ (Proved above)}$$

$$\angle B'AC' = \angle BAC \text{ (Common)}$$

$$\therefore \triangle AB'C' \sim \triangle ABC \text{ (AA similarity criterion)}$$

$$\Rightarrow \frac{AB'}{AB} = \frac{B'C'}{BC} = \frac{AC'}{AC} \quad \dots (1)$$

In $\triangle AA_2B'$ and $\triangle AA_3B$,

$$\angle A_2AB' = \angle A_3AB \text{ (Common)}$$

$$\angle AA_2B' = \angle AA_3B \text{ (Corresponding angles)}$$

$$\therefore \triangle AA_2B' \sim \triangle AA_3B \text{ (AA similarity criterion)}$$

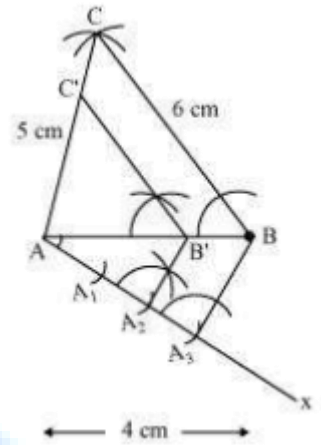
$$\Rightarrow \frac{AB'}{AB} = \frac{AA_2}{AA_3}$$

$$\Rightarrow \frac{AB'}{AB} = \frac{2}{3} \quad \dots (2)$$

From equations (1) and (2), we obtain

$$\Rightarrow \frac{AB'}{AB} = \frac{B'C'}{BC} = \frac{AC'}{AC} = \frac{2}{3} \Rightarrow AB' = \frac{2}{3} AB, B'C' = \frac{2}{3} BC, AC' = \frac{2}{3} AC$$

This justifies the construction.



Q.3 Construct a triangle with sides 5 cm, 6 cm and 7 cm and then another triangle whose sides are $\frac{7}{5}$ of the corresponding sides of the first triangle. Give the justification of the construction.

Answer :

Step 1

Draw a line segment AB of 5 cm. Taking A and B as centre, draw arcs of 6 cm and 5cm radius respectively. Let these arcs intersect each other at point C. ΔABC is the required triangle having length of sides as 5 cm, 6 cm, and 7 cm respectively.

Step 2

Draw a ray AX making acute angle with line AB on the opposite side of vertex C.

Step 3

Locate 7 points, $A_1, A_2, A_3, A_4, A_5, A_6, A_7$ (as 7 is greater between 5 and 7), on line AX such that $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_6A_7$.

Step 4

Join BA_5 and draw a line through A_7 parallel to BA_5 to intersect extended line segment AB at point B' .

Step 5

Draw a line through B' parallel to BC intersecting the extended line segment AC at C' . $\Delta AB'C'$ is the required triangle.

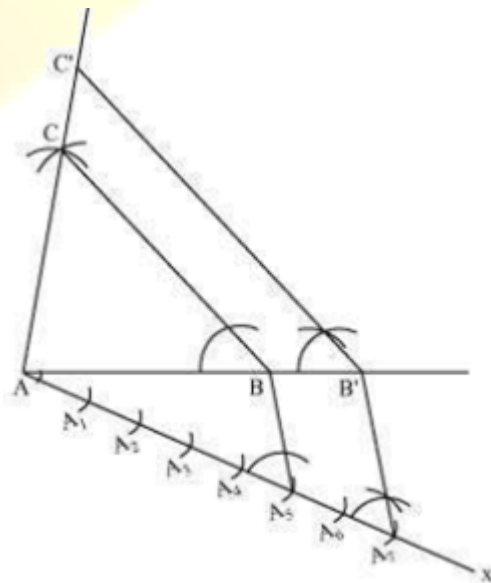
Justification

The construction can be justified by proving that

$$\Rightarrow AB' = \frac{7}{5} AB, B'C' = \frac{7}{5} BC, AC' = \frac{7}{5} AC$$

In ΔABC and $\Delta AB'C'$,

$$\angle ABC = \angle AB'C' \text{ (Corresponding angles)}$$



$$\angle BAC = \angle B'AC' \text{ (Common)}$$

$\therefore \Delta ABC \sim \Delta AB'C'$ (AA similarity criterion)

$$\Rightarrow \frac{AB}{AB'} = \frac{BC}{B'C'} = \frac{AC}{AC'} \quad \dots (1)$$

In ΔAA_5B and $\Delta AA_7B'$,

$$\angle A_5AB = \angle A_7AB' \text{ (Common)}$$

$$\angle AA_5B = \angle AA_7B' \text{ (Corresponding angles)}$$

$\therefore \Delta AA_5B \sim \Delta AA_7B'$ (AA similarity criterion)

$$\Rightarrow \frac{AB}{AB'} = \frac{AA_5}{AA_7}$$

$$\Rightarrow \frac{AB'}{AB} = \frac{5}{7} \quad \dots (2)$$

From equations (1) and (2), we obtain

$$\Rightarrow \frac{AB}{AB'} = \frac{BC}{B'C'} = \frac{AC}{AC'} = \frac{5}{7}$$

$$\Rightarrow AB' = \frac{7}{5} AB, B'C' = \frac{7}{5} BC, AC' = \frac{7}{5} AC$$

This justifies the construction.

Q.4 Construct an isosceles triangle whose base is 8 cm and altitude 4 cm and then another triangle whose sides are $1\frac{1}{2}$ times the corresponding sides of the isosceles triangle. Give the justification of the construction.

Sol: Let us assume that ΔABC is an isosceles triangle having CA and CB of equal lengths, base AB of 8 cm, and AD is the altitude of 4 cm.

A $\Delta AB'C'$ whose sides are $\frac{3}{2}$ times of ΔABC can be drawn as follows.

Step 1

Draw a line segment AB of 8 cm. Draw arcs of same radius on both sides of the line segment while taking point A & B as its centre. Let these arcs intersect each other at O & O'. Join OO'. Let OO' intersect AB at D.

Step 2

Taking D as centre, draw an arc of 4 cm radius which cuts the extended line segment OO' at point C.

An isosceles ΔABC is formed, having CD (altitude) as 4 cm and AB (base) as 8 cm.

Step 3

Draw a ray AX making an acute angle with line segment AB on the opposite side of vertex C.

Step 4

Locate 3 points (as 3 is greater between 3 and 2) $A_1, A_2,$ and A_3 on AX such that $AA_1 = A_1A_2 = A_2A_3$.

Step 5

Join BA_2 and draw a line through A_3 parallel to BA_2 to intersect extended line segment AB at point B' .

Step 6

Draw a line through B' parallel to BC intersecting the extended line segment AC at C' . $\Delta AB'C'$ is the required triangle.

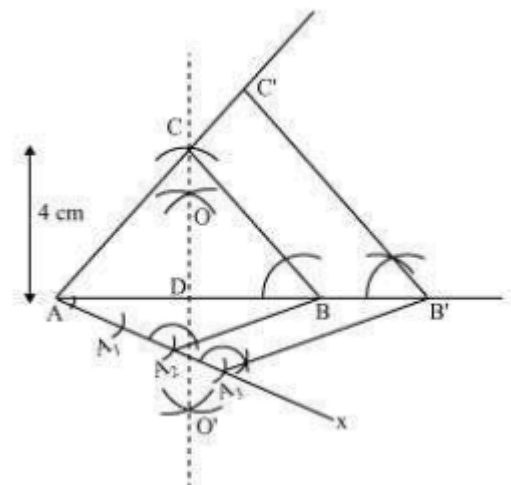
Justification

The construction can be justified by proving that

$$\Rightarrow AB' = \frac{3}{2} AB, B'C' = \frac{3}{2} BC, AC' = \frac{3}{2} AC$$

In ΔABC and $\Delta AB'C'$,

$$\angle ABC = \angle AB'C' \text{ (Corresponding angles)}$$



$$\angle BAC = \angle B'AC' \text{ (Common)}$$

$\therefore \Delta ABC \sim \Delta AB'C'$ (AA similarity criterion)

$$\Rightarrow \frac{AB'}{AB} = \frac{B'C'}{BC} = \frac{A'C'}{AC} \quad \dots (1)$$

In ΔAA_2B and $\Delta AA_3B'$,

$$\angle A_2AB = \angle A_3AB' \text{ (Common)}$$

$$\angle AA_2B = \angle AA_3B' \text{ (Corresponding angles)}$$

$\therefore \Delta AA_2B \sim \Delta AA_3B'$ (AA similarity criterion)

$$\begin{aligned} \Rightarrow \frac{AB}{AB'} &= \frac{AA_2}{AA_3} \\ \Rightarrow \frac{AB}{AB'} &= \frac{2}{3} \quad \dots(2) \end{aligned}$$

From equations (1) and (2), we obtain

$$\begin{aligned} \Rightarrow \frac{AB}{AB'} &= \frac{BC}{B'C'} = \frac{AC}{AC'} = \frac{2}{3} \\ \Rightarrow AB' &= \frac{2}{3} AB, B'C' = \frac{3}{2} BC, AC' = \frac{3}{2} AC \end{aligned}$$

This justifies the construction.

Q.5 Draw a triangle ABC with side BC = 6 cm, AB = 5 cm and $\angle ABC = 60^\circ$. Then construct a triangle whose sides are $\frac{3}{4}$ of the corresponding sides of the triangle ABC. Give the justification of the construction.

Sol: A $\Delta A'BC'$ whose sides are $\frac{3}{4}$ of the corresponding sides of ΔABC can be drawn as follows.

Step 1

Draw a ΔABC with side $BC = 6$ cm, $AB = 5$ cm and $\angle ABC = 60^\circ$.

Step 2

Draw a ray BX making an acute angle with BC on the opposite side of vertex A .

Step 3

Locate 4 points (as 4 is greater in 3 and 4), B_1, B_2, B_3, B_4 , on line segment BX .

Step 4

Join B_4C and draw a line through B_3 , parallel to B_4C intersecting BC at C' .

Step 5

Draw a line through C' parallel to AC intersecting AB at A' . $\Delta A'BC'$ is the required triangle.

Justification

The construction can be justified by proving

$$\Rightarrow A'B = \frac{3}{4} AB, B'C' = \frac{3}{4} BC, AC' = \frac{3}{4} AC$$

In $\Delta A'BC'$ and ΔABC ,

$$\angle A'C'B = \angle ACB \text{ (Corresponding angles)}$$

$$\angle A'BC' = \angle ABC \text{ (Common)}$$

$$\therefore \Delta A'BC' \sim \Delta ABC \text{ (AA similarity criterion)}$$

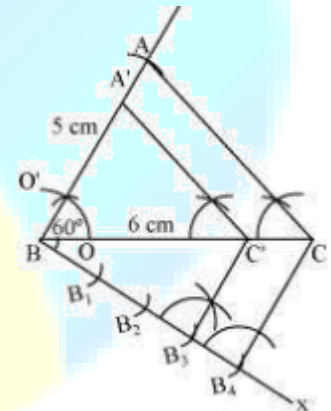
$$\Rightarrow \frac{AB}{A'B} = \frac{BC}{B'C'} = \frac{AC}{AC'} \quad \dots (1)$$

In $\Delta BB_3C'$ and ΔBB_4C ,

$$\angle B_3BC' = \angle B_4BC \text{ (Common)}$$

$$\angle BB_3C' = \angle BB_4C \text{ (Corresponding angles)}$$

$$\therefore \Delta BB_3C' \sim \Delta BB_4C \text{ (AA similarity criterion)}$$



$$\Rightarrow \frac{BB'}{BC} = \frac{BB_3}{BB_4}$$

$$\Rightarrow \frac{BC'}{BC} = \frac{3}{4} \quad \dots(2)$$

From equations (1) and (2), we obtain

$$\frac{A'B}{AB} = \frac{BC'}{BC} = \frac{A'C'}{AC} = \frac{2}{3}$$

$$\Rightarrow A'B = \frac{2}{3} AB, BC' = \frac{2}{3} BC, AC' = \frac{2}{3} AC$$

This justifies the construction.

Q.6 Draw a triangle ABC with side BC = 7 cm, $\angle B = 45^\circ$, $\angle A = 105^\circ$. Then, construct a triangle whose sides are $\frac{4}{3}$ times the corresponding side of ΔABC . Give the justification of the construction.

Sol:

$$\angle B = 45^\circ, \angle A = 105^\circ$$

Sum of all interior angles in a triangle is 180° .

$$\angle A + \angle B + \angle C = 180^\circ$$

$$105^\circ + 45^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 150^\circ$$

$$\angle C = 30^\circ$$

The required triangle can be drawn as follows.

Step 1

Draw a ΔABC with side BC = 7 cm, $\angle B = 45^\circ$, $\angle C = 30^\circ$.

Step 2

Draw a ray BX making an acute angle with BC on the opposite side of vertex A.

Step 3

Locate 4 points (as 4 is greater in 4 and 3), B_1, B_2, B_3, B_4 , on BX.

Step 4

Join B_3C . Draw a line through B_4 parallel to B_3C intersecting extended BC at C' .

Step 5

Through C' , draw a line parallel to AC intersecting extended line segment at A' .

$\Delta A'BC'$ is the required triangle.

Justification

The construction can be justified by proving that

In ΔABC and $\Delta A'BC'$,

$$\angle ABC = \angle A'BC' \text{ (Common)}$$

$$\angle ACB = \angle A'C'B \text{ (Corresponding angles)}$$

$$\therefore \Delta ABC \sim \Delta A'BC' \text{ (AA similarity criterion)}$$

$$\Rightarrow \frac{AB}{A'B} = \frac{BC}{B'C'} = \frac{AC}{A'C'} \quad \dots (1)$$

In ΔBB_3C and $\Delta BB_4C'$,

$$\angle B_3BC = \angle B_4BC' \text{ (Common)}$$

$$\angle BB_3C = \angle BB_4C' \text{ (Corresponding angles)}$$

$$\therefore \Delta BB_3C \sim \Delta BB_4C' \text{ (AA similarity criterion)}$$

$$\Rightarrow \frac{BC}{BC'} = \frac{BB_3}{BB_4}$$

$$\Rightarrow \frac{BC}{BC'} = \frac{3}{4} \quad \dots(2)$$

On comparing equations (1) and (2), we obtain

$$\frac{AB}{A'B} = \frac{BC}{BC'} = \frac{AC}{A'C'} = \frac{3}{4}$$

$$\Rightarrow A'B = \frac{4}{3} AB, BC' = \frac{4}{3} BC, A'C' = \frac{4}{3} AC$$

This justifies the construction.

Q.7 Draw a right triangle in which the sides (other than hypotenuse) are of lengths 4 cm & 3 cm. the construct another triangle whose sides are $\frac{5}{3}$ times the corresponding sides of the given triangle.

Give the justification of the construction.

Sol: It is given that sides other than hypotenuse are of lengths 4 cm and 3 cm. Clearly, these will be perpendicular to each other. The required triangle can be drawn as follows.

Step 1 Draw a line segment $AB = 4$ cm. Draw a ray SA making 90° with it.

Step 2

Draw an arc of 3 cm radius while taking A as its centre to intersect SA at C . Join BC .

$\triangle ABC$ is the required triangle.

Step 3

Draw a ray AX making an acute angle with AB , opposite to vertex C .

Step 4

Locate 5 points (as 5 is greater in 5 and 3), A_1, A_2, A_3, A_4, A_5 , on line segment AX

such that $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5$.

Step 5

Join A_3B . Draw a line through A_5 parallel to A_3B intersecting extended line segment AB at B' .

Step 6

Through B' , draw a line parallel to BC intersecting extended line segment AC at C' .

$\triangle AB'C'$ is the required triangle.

Justification

The construction can be justified by proving that $\Rightarrow AB' = \frac{5}{3} AB, B'C' = \frac{5}{3} BC, AC' = \frac{5}{3} AC$

In $\triangle ABC$ and $\triangle AB'C'$,

$$\angle ABC = \angle AB'C' \text{ (Corresponding angles)}$$

$$\angle BAC = \angle B'AC' \text{ (Common)}$$

$$\therefore \triangle ABC \sim \triangle AB'C' \text{ (AA similarity criterion)}$$

$$\Rightarrow \frac{AB}{A'B'} = \frac{BC}{B'C'} = \frac{AC}{A'C'} \quad \dots (1)$$

In $\triangle AA_3B$ and $\triangle AA_5B'$,

$$\angle A_3AB = \angle A_5AB' \text{ (Common)}$$

$$\angle AA_3B = \angle AA_5B' \text{ (Corresponding angles)}$$

$$\therefore \triangle AA_3B \sim \triangle AA_5B' \text{ (AA similarity criterion)}$$

$$\Rightarrow \frac{AB}{AB'} = \frac{AA_3}{AA_5}$$

$$\Rightarrow \frac{AB}{AB'} = \frac{3}{5} \quad \dots (2)$$

$$\frac{AB}{AB'} = \frac{BC}{B'C'} = \frac{AC}{A'C'} = \frac{3}{5}$$

$$\Rightarrow AB' = \frac{5}{3} AB, B'C' = \frac{5}{3} BC, A'C' = \frac{5}{3} AC$$

This justifies the construction.