

Board – ICSE

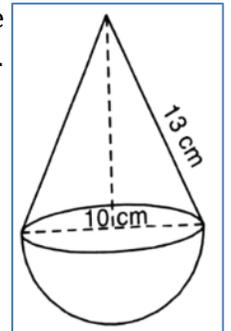
Class – 10<sup>th</sup>

Topic – Sphere, Hemisphere and Shell

1. The surface area of a solid metallic sphere is  $616 \text{ cm}^2$ . It is melted and recast into smaller sphere of 3.5 cm diameter. How many such spheres can be obtained? [Ans: 64]
2. A hemispherical bowl of 14.4 cm diameter is filled completely with chocolate sauce. This sauce is poured into an inverted cone of 9.6 cm radius. Find height of cone. [Ans: 8.1 cm]
3. A solid cone of 5 cm radius and 8 cm height is melted and made into small spheres of 0.5 cm radius. Find the number of spheres formed. [Ans: 400]
4. The given figure represents a hemisphere surmounted by a conical block of wood. The diameter A of their bases is 10 cm each other and the slant height of the cone is 13 cm. Calculate:

- (i) The height of the cone, and
- (ii) The volume of the solid.

[Ans: 12 cm]

[Ans:  $602.38 \text{ cm}^3$ ]

5. A tent is in the form of a right circular cone. Its height is 4 m and base diameter is 10.5 m. If it can accommodate 15 persons, how many cubic metres of air is available for each person? [Ans:  $7.7 \text{ m}^3$ ]
6. A sphere has a radius of 10.5 cm. Find its
  - a) Volume, and [Ans:  $4,851 \text{ cm}^3$ ]
  - b) Surface area. [Ans:  $1,386 \text{ cm}^2$ ]
7. A spherical ball of a metal, 6 cm in diameter is melted and recast into three spherical balls. Diameters of two balls are 3 cm and 4 cm. What is diameter of the third ball? [Ans: 5 cm]
8. What is the least number of solid metallic spheres each of 4 cm radius that should be melted and recast to form a hollow sphere of 24 cm outer diameter and of 2 cm uniform thickness? [Ans: 12]
9. A vessel is in the form of an inverted cone. Its height is 8 cm and the radius of its top which is open is 5 cm. It is filled with water up to the rim. When lead shots, each of which is a sphere of 0.5 cm radius, are dropped into the vessel, one fourth of the water flows out. Find the number of leads shots dropped into the vessel. (Take  $\pi = 22/7$ ) [Ans: 100]
10. Find the total surface area of a cone of 6 cm radius and 8 cm slant height. [Ans:  $264 \text{ cm}^2$ ]
11. A conical tent, 6 m in diameter and 4 m high, is made of canvas. How many such tents can be made from 1,000 m long, 110 cm wide canvas, allowing 10% for wastage? [Ans: 21]
12. A solid cylinder of radius 12 cm and height 20 cm is melted into solid spheres of radius 0.5 cm. Find the number of solid spheres made. [Ans: 17280]
13. A hollow cylinder of outer radius 15 cm and inner radius 5 cm and height 20 cm is recast into solid cones of radius 4 cm and perpendicular height 10 cm. Find the number of cones formed. [Ans: 75]
14. The area of the curved surface of a solid cylinder is  $2200 \text{ cm}^2$  and the circumference of the base is 55 cm. Find:

- a) Height of the cylinder, and [Ans: 40cm]  
b) Volume of the cylinder. [Ans: 9625 cm<sup>3</sup>]
15. How many revolutions will a roller of radius 0.7 m and length 2.5 m make to level a field 770 m × 350 m? [Ans: 24500]
16. A cube is immersed completely in a cylinder containing water. If the level of water rises by 7 cm and the base radius of the cylinder is 22 cm, find the length of the cube. [Ans: 22 cm]
17. Find the cost of painting a hollow cylinder of outer diameter 14 m, thickness 7 cm and height 7 m at Rs, 100 per m<sup>2</sup>. [Ans: Rs. 64,372]
18. A solid cylinder has its radius and height in the ratio 1:3. If its volume is 404.25 cm<sup>3</sup>. Find its radius. [Ans: 3.5 cm]
19. Find the volume of a cylinder which has a base diameter 14 cm and height 24 cm. [Ans: 3696 cm<sup>3</sup>]
20. The total surface area of a cylinder is 264 cm<sup>2</sup>. Find its volume if its height is 5 cm more than its radius. [Ans: 357.25 cm<sup>3</sup>]
21. The volume of a cylinder of height 4 cm is  $196\pi$  cm<sup>3</sup>. Find its lateral surface area and its total surface area. [Ans: 176 cm<sup>2</sup>; 484 cm<sup>2</sup>]
22. The volume of a conical tent is 1,232 m<sup>3</sup> and the area of its base is 154 m<sup>2</sup>. Calculate
- a) The radius of the floor [Ans: 7m]  
b) The height of the tent, and [Ans: 25 m]  
c) The length of canvas required to cover this tent if its width is 2 m. [Ans: 275 m]