

Exam Preparation 1

Exam : ICSE Sub. : Maths 10th Topic : Probability

$$P(A) = \frac{\text{Number of outcomes favourable to A}}{\text{Numbers of possible outcomes of the experiment}}$$

Practical Application

Tossing of unbiased coin	❖ Two outcomes: Head (H) and Tail (T)
Tossing of 2 unbiased coin simultaneously	❖ Four outcomes: HH,HT,TH,TT
Tossing of 3 unbiased coin simultaneously	❖ Eight outcomes: HHH,HHT,HTH,HTT,THH,THT,TTH,TTT
Throwing of unbiased die	❖ 6 outcomes: numbers 1,2,3,4,5 and 6
Throwing of 2 unbiased dice simultaneously.	❖ 36 outcomes: (1,1),(1,2),.....(6,5),(6,6)
Shuffling of a deck of cards	❖ A "standard" deck of playing cards consists of 52 Cards in each of the 4 suits of Spades, Hearts, Diamonds, and Clubs ❖ Cards of Spades and clubs are black cards. ❖ Cards of hearts and diamonds are red cards. ❖ Each suit contains 13 cards: Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King. ❖ King, Queen and Jack (or Knaves) are face cards.

The **sum of the probabilities** of all the elementary events of an experiment is 1.

The event \bar{A} representing 'not A', is called the complement of the event A. We also say that \bar{A} and A are complementary events.

Bounds of P(E) : $0 \leq P(E) \leq 1$; **Probability can never be negative.**

Nature of the events	Probability
Sure or certain events	One
Impossible events	Zero

1. Cards bearing numbers 2, 4, 6, 8, 10, 12, 14, 16, 18 and 20 are kept in a bag. A card is drawn at random from this bag. Find a probability of getting a card which is: (i) a prime number (ii) a number divisible by 4 (iii) a number that is multiple of 6 (iv) an odd number **(ICSE 2018)**
2. Sixteen cards are labeled as a,b,c, ..., m,n,o,p. They are put in a box and shuffled. A boy is asked to draw a card from the box. What is the probability that the card draw is: (i) A Vowel (ii) A Consonant (iii) None of the letters of the word median. **(ICSE 2017)**
3. A game of number has cards marked with 11, 12, 13,.....39,40. A card is drawn at random. Find the probability that the number on the card drawn is: i) A perfect square ii) Divisible by 7. **(ICSE 2016)**
4. A bag contain 5 white balls, 6 red balls and 9 green balls. A ball is drawn at random from the bag, Find the probability that the ball drawn is: (i) a green ball (ii) a white or a red ball (iii) is neither a green ball nor a white ball. **(ICSE 2015)**
5. A die has 6 faces marked by the given numbers as shown below: 1, 2, 3, -1, -2, -3. The die is thrown once. What is the probability of getting? (i) A positive integer (ii) An integer greater than -3 (iii) The smallest integer **(ICSE 2014)**
6. A box contain some black balls and 30 white balls. If the probability of drawing a black ball is two-fifths of a white ball, find the number of black balls in the box. **(ICSE 2013)**
7. Two coins are tossed once; Find the probability of getting: (i) 2 heads (ii) At least 1 tail **(ICSE 2012)**
8. From a pack of 52 playing cards all cards whose numbers are multiples of 3 are removed. A card is now drawn at random. What is the probability that the card drawn is; (i) a face card (ii) an even number red card. **(ICSE 2011)**

Question: Three coins are tossed. What is the probability of getting at most two tails?

Solution: Total number of outcomes possible when a coin is tossed = 2 (\because Head or Tail)

Hence, total number of outcomes possible when 3 coins are tossed, $n(S) = 2 \times 2 \times 2 = 8$

(\because i.e., $S = \{TTT, TTH, THT, HTT, THH, HTH, HHT, HHH\}$)

E = event of getting at most two Tails = $\{TTH, THT, HTT, THH, HTH, HHT, HHH\}$

Hence, $n(E) = 7$ $P(E) = \frac{n(E)}{n(S)} = \frac{7}{8}$

Question: A card is drawn from a well shuffled pack of 52 cards. Find the probability of: non-face card of black colour.

Solution: Cards of spades and clubs are black cards. Number of spades = 13 and Number of clubs = 13 Therefore, total number of black card out of 52 cards = $13 + 13 = 26$

Number of face cards in each suits namely spades and clubs = $3 + 3 = 6$ Therefore, total number of non-face card of black colour out of 52 cards = $26 - 6 = 20$. Therefore, probability of getting 'non-face card of black colour'. $P(J) = \frac{n(E)}{n(S)} = \frac{20}{52} = \frac{5}{13}$