## MATHEMATICS

Board - ICSE
$\square$
Class - IX
Topic - Statistics

1. Following data gives the number of children in 40 families :
$1,2,6,5,1,3,2,6,2,3,4,2,0,4,4,3,2,2,0,0,1,2,2,4,4,3,2,1,0,5,1,2,4,3,4,1,1,6,2,2$. Represent it in the form of a frequency distribution.

## Solution:

Below is given a frequency distribution of the given data.

| No. of Children | Tally-Marks | Frequency |
| :---: | :---: | :---: |
| 0 | IIII | 4 |
| 1 | 씨 II | 7 |
| 2 | 씨 씨II | 12 |
| 3 | 씨 | 5 |
| 4 | 씨 II | 7 |
| 5 | II | 2 |
| 6 | III | 3 |

2. The weekly wages (in rupees) of 30 workers in a factory are given below :
$630,635,690,610,635,636,639,645,698,690,620,660,632,633,655,645,604,608,612,640,685$, $635,636,678,640,668,690,606,640,690$. Represent the data in the form of a frequency distribution with class size 10.

## Solution:

From the given data, Lowest data $=604$ and Largest data $=698$
$\therefore$ Range of data $=698-604=94$
Frequency distribution of the given data is as follows:

| Class Interval | Tally-Marks | Frequency |
| :---: | :---: | :---: |
| 600-610 | III | 3 |
| 610-620 | 11 | 2 |
| 620-630 | 1 | 1 |
| 630-640 | 发 IIII | 9 |
| 640-650 | ky | 5 |
| 650-660 | 1 | 1 |
| 660-670 | 11 | 2 |
| 670-680 | I | 1 |
| 680-690 | I | 1 |
| 690-700 | k\| | 5 |
| Total |  | 30 |

3. Convert the following frequency distribution to exclusive form : Use this table to find :

| Class Interval | Frequency |
| :---: | :---: |
| $30-34$ | 7 |
| $35-39$ | 9 |
| $40-44$ | 13 |
| $45-49$ | 6 |
| $50-54$ | 3 |
| $55-59$ | 10 |

(i) The true class limits of the fourth class interval.
(ii) The class boundaries of the fifth class interval.
(iii) The class mark of the third class interval.
(iv) The class size of the sixth class interval.

## Solution:

Frequency distribution to exclusive form of the given frequency distribution is as follows:

| Class Interval | Frequency |
| :---: | :---: |
| $29.5-34.5$ | 7 |
| $34.5-39.5$ | 9 |
| $39.5-44.5$ | 13 |
| $44.5-49.5$ | 6 |
| $49.5-54.5$ | 3 |
| $54.5-59.5$ | 10 |

(i) The true class limits of the fourth class interval is $44.5-49.5$.
(ii) The class boundaries of the fifth class interval is $49.5-54.5$.
(iii) The class mark of the third class interval $\frac{39.5+44.5}{2}=\frac{84}{2}=42$
(iv) The class size of the sixth class interval $=59.5-54.5=5$
4. Find the actual lower class limits and upper class limits of the classes: 10-19, 20-29, 30-39 and 40-49.

## Solution:

Classes are 10-19, 20-29, 30-39 and 40-49.
Difference between upper limit of one class and lower limit of next class $=1$
$\therefore$ Adjustment of factor $=\frac{1}{2}=0.5$
Subtracting the adjustment factor from the lower limits and adding it to all the upper limits.

Thus, classes become, 9.5-19.5, 19.5-29.5, 29.5-39.5 and 39.5-49.5.
Hence, actual lower limits are 9.5, 19.5, 29.5 and 39.5 and actual upper limits are 19.5, 29.5, 29.5 and 49.5.
5. Construct a frequency distribution table from the following cumulative frequency distribution :
(i)

| Class Interval | Cumulative Frequency |
| :---: | :---: |
| $10-19$ | 8 |
| $20-29$ | 19 |
| $30-39$ | 23 |
| $40-49$ | 30 |

(ii)

| Class Interval | Cumulative Frequency |
| :---: | :---: |
| $5-10$ | 18 |
| $10-15$ | 30 |
| $15-20$ | 46 |
| $20-25$ | 73 |
| $25-30$ | 90 |

Solution:
(i) Frequency Distribution Table is as follows :

| Class Interval | Cumulative Frequency | Frequency $f$ |
| :---: | :---: | :---: |
| $10-19$ | 8 | 8 |
| $20-29$ | 19 | $19-8=11$ |
| $30-39$ | 23 | $23-19=4$ |
| $40-49$ | 30 | $30-23=7$ |
|  | Total | 30 |

(ii) Frequency Distribution Table is as follows :

| Class Interval | Cumulative Frequency | Frequency $f$ |
| :---: | :---: | :---: |
| $5-10$ | 18 | 18 |
| $10-15$ | 30 | $30-18=12$ |
| $15-20$ | 46 | $46-30=16$ |
| $20-25$ | 73 | $73-46=27$ |
| $25-30$ | 90 | $90-73=17$ |
|  | Total | 90 |

6. Construct the frequency distribution table from the following cumulative frequency table :
(i) State the number of students in the age group 10-13.
(ii) State the age group which has the least number of students.

| Ages | Number of Students |
| :---: | :---: |
| Below 4 | 0 |
| Below 7 | 85 |
| Below 10 | 140 |
| Below 13 | 243 |
| Below 16 | 300 |

## Solution:

Since, there is no students below age of 4 years, hence starting the classes from lower limits as 4 .
(i) Number of students in the age group 10-13 $=103$.
(ii) Age group which has the least number of students is 7-10.

| Ages | No. of Students | Frequency $f$ |
| :---: | :---: | :---: |
| $4-7$ | 85 | 85 |
| $7-10$ | 140 | $140-85=55$ |
| $10-13$ | 243 | $243-140=103$ |
| $13-16$ | 300 | $300-243=57$ |
|  | Total | 300 |

7. Fill in the blanks in the following table.

| Class Interval | Frequency | Cumulative Frequency |
| :---: | :---: | :---: |
| $25-34$ | $\ldots$ | 15 |
| $35-44$ | $\ldots$ | 28 |
| $45-54$ | 21 | $\ldots$ |
| $55-64$ | 16 | $\cdots$ |
| $65-74$ | $\ldots$ | 73 |
| $75-84$ | 12 | $\ldots$ |

Solution:

| Class Interval | Frequency | Cumulative Frequency |
| :---: | :---: | :---: |
| $25-34$ | $\underline{15}$ | 15 |
| $35-44$ | $\frac{28-15=13}{21}$ | 28 |
| $45-54$ | 16 | $\frac{28+21=49}{49+16=65}$ |
| $55-64$ | $\frac{73-65=8}{12}$ | $\underline{73+12=85}$ |
| $65-74$ |  |  |

8. Construct a histogram for the following frequency distribution :

| Daily earning <br> (in Rs.) | $80-120$ | $120-160$ | $160-200$ | $200-240$ |
| :---: | :---: | :---: | :---: | :---: |
| Number of <br> Workers | 4 | 8 | 10 | 2 |

## Solution:

Taking daily earnings (in Rs.) along x axis and number of workers along y axis. Below is given a histogram of the given data. Scale $1 \mathrm{~cm}=2$ workers.

## MATHEMATICS


9. Draw a histogram for the following frequency distribution :

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 4 | 9 | 5 | 12 | 3 |

## Solution:

Taking marks along $x$-axis and number of students along $y$-axis. Below is given the histogram of the given data. Scale $1 \mathrm{~cm}=2$ students.

10. The following table shows the marks obtained by the students of a class in an examination. Draw a frequency polygon.

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No, of <br> Students | 15 | 32 | 55 | 35 | 13 |

## Solution:

Taking marks along $x$-axis and number of students, along $y$-axis. First we draw a histogram and then by joining the mid-points of consecutive rectangle, we will get a frequency polygon. Scale: $1 \mathrm{~cm}=10$ students.

11. Each of the 25 students in a class was given a home assignment comprising 10 questions in mathematics. The data given below, show the number of questions solved and submitted by individual students on the next day.
$1,4,5,6,0,9,3,2,3,4,6,4,5,2,7,5,2,2,3,5,1,0,7,6,3$.
(i) Taking classes as 0-2, 2-4, 4-6 ... etc., make a frequency table for the above distribution.
(ii) Draw frequency polygon to represent the given data.

## Solution:

(i) Frequency distribution table for the above data is as follows:

| Class Interval | Tally Marks | Frequency |
| :---: | :---: | :---: |
| $0-2$ | IIII | 4 |
| $2-4$ | kyll\| | 8 |
| $4-6$ | kyl II | 7 |
| $6-8$ | kil | 5 |
| $8-10$ | \| | 1 |
|  | Total | 25 |

(ii) To draw frequency polygon :
(a) Draw the histogram for the given data by taking class intervals along $x$-axis and frequency along y -axis.
(b) Mark the mid-point of top of each rectangle of histogram.
(c) Mark the mid-point of immediately higher class interval (i.e. 10-12) with frequency zero.
(d) Join the consecutive mid-points marked by straight lines. Also, join the mid-point of immediately lower class with frequency zero to midpoint of rectangle for 0-2. Required frequency polygon is as follow.


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