

Board – NCERT

Class – 10th

Topic – Quadratic 4.1

**Q.1** Check whether the following are quadratic equations:

(i)  $(x + 1)^2 = 2(x - 3)$

(ii)  $x^2 - 2x = (-2)(3 - x)$

(iii)  $(x - 2)(x + 1) = (x - 1)(x + 3)$

(iv)  $(x - 3)(2x + 1) = x(x + 5)$

(v)  $(x - 3)(2x - 1) = (x + 5)(x - 1)$

(viii)  $x^3 - 4x^3 - x + 1 = (x - 2)^3$

**Sol:** (i)  $(x + 1)^2 = 2(x - 3)$

$$(x + 1)^2 = 2(x - 3) \Rightarrow x^2 + 2x + 1 = 2x - 6 \Rightarrow x^2 + 7 = 0$$

It is of the form  $ax^2 + bx + c = 0$

Hence, the given equation is a quadratic equation.

(ii)  $x^2 - 2x = (-2)(3 - x)$

$$x^2 - 2x = (-2)(3 - x) \Rightarrow x^2 - 2x = -6 + 2x \Rightarrow x^2 - 4x + 6 = 0$$

It is of the form  $ax^2 + bx + c = 0$

Hence, the given equation is a quadratic equation.

(iii)  $(x - 2)(x + 1) = (x - 1)(x + 3)$

$$(x - 2)(x + 1) = (x - 1)(x + 3) \Rightarrow x^2 - x - 2 = x^2 - 2x - 3 \Rightarrow 3x - 1 = 0$$

It is not of the form  $ax^2 + bx + c = 0$

Hence, the given equation is not a quadratic equation.

(iv)  $(x - 3)(2x + 1) = x(x + 5)$

$$(x - 3)(2x + 1) = x(x + 5)$$

$$\Rightarrow 2x^2 - 5x - 3 = x^2 + 5 \Rightarrow x^2 - 10x - 3 = 0$$

It is of the form  $ax^2 + bx + c = 0$

Hence, the given equation is a quadratic equation.

$$(v) (x - 3)(2x - 1) = (x + 5)(x - 1)$$

$$(x - 3)(2x - 1) = (x + 5)(x - 1) \Rightarrow 2x^2 - 7x + 3 = x^2 + 4x - 5 \Rightarrow x^2 - 11x + 8 = 0$$

It is of the form  $ax^2 + bx + c = 0$

Hence, the given equation is a quadratic equation.

$$(vi) x^2 + 3x + 1 = (x - 2)^2$$

$$x^2 + 3x + 1 = (x - 2)^2 \Rightarrow x^2 + 3x + 1 = x^2 + 4 - 4x \Rightarrow 7x - 3 = 0$$

It is not of the form  $ax^2 + bx + c = 0$

Hence, the given equation is not a quadratic equation.

$$(vii) (x + 2)^3 = 2x(x^2 - 1)$$

$$(x + 2)^3 = 2x(x^2 - 1) \Rightarrow x^2 + 3x + 1 = x^2 + 4 - 4x \Rightarrow 7x - 3 = 0$$

It is not of the form  $ax^2 + bx + c = 0$

Hence, the given equation is not a quadratic equation.

$$(viii) x^3 - 4x^3 - x + 1 = (x - 2)^3$$

$$x^3 - 4x^3 - x + 1 = (x - 2)^3 \Rightarrow x^3 - 4x^3 - x + 1 = x^3 - 8 - 6x^2 + 12x \Rightarrow 2x^2 - 13x + 9 = 0$$

It is of the form  $ax^2 + bx + c = 0$

Hence, the given equation is a quadratic equation.

**Q.2** Represent the following situations in the form of quadratic equations.

(i) The area of a rectangular plot is  $528 m^2$ . The length of the plot (in metres) is one more than twice its breadth. We need to find the length and breadth of the plot.

(ii) The product of two consecutive positive integers is 306 . We need to find the integers.

(iii) Rohan's mother is 26 years older than him. The product of their ages (in years) 3 years from now will be 360 . We would like to find Rohan's present age.

(vi) A train travels a distance of 480 km at a uniform speed. If the speed had been 8 km/h less, then it would have taken 3 hours more to cover the same distance. We need to find the speed of the train.

**Sol:** (i) The area of a rectangular plot is  $528 m^2$ . The length of the plot (in metres) is one more than twice its breadth. We need to find the length and breadth of the plot.

Let the breadth of the plot be  $xm$ .

Hence, the length of the plot is  $(2x + 1)m$ .

Area of a rectangle = Length  $\times$  Breadth

$$\therefore 528 = x(2x + 1) \Rightarrow 2x^2 + x - 528 = 0$$

(ii) The product of two consecutive positive integers is 306 . We need to find the integers.

Let the consecutive integers be  $x$  and  $x + 1$ .

It is given that their product is 306 .

$$\therefore x(x + 1) = 306 \Rightarrow x^2 + x - 306 = 0$$

(iii) Rohan's mother is 26 years older than him. The product of their ages (in years) 3 years from now will be 360 . We would like to find Rohan's present age.

Let Rohan's age be  $x$ .

Hence, his mother's age =  $x + 26$

3 years hence,

Rohan's age =  $x + 3$

Mother's age =  $x + 26 + 3 = x + 29$

It is given that the product of their ages after 3 years is 360 .

$$\therefore (x + 3)(x + 29) = 360$$

$$\Rightarrow x^2 + 32x - 273 = 0$$

(vi) A train travels a distance of 480 km at a uniform speed. If the speed had been 8 km/h less, then it would have taken 3 hours more to cover the same distance. We need to find the speed of the train.

Let the speed of train be  $x$  km/h.

$$\text{Time taken to travel 480 km} = \frac{480}{x \text{ hrs}}$$

$$\text{In second condition, let the speed of train} = \frac{(x-8) \text{ km}}{h}$$

It is also given that the train will take 3 hours to cover the same  $\left(\frac{480}{x} + 3\right)$  distance.

Therefore, time taken to travel 480 km = hrs

Speed  $\times$  Time = Distance

$$(x - 8)\left(\frac{480}{x} + 3\right) = 480 \Rightarrow 480 + 3x - \frac{3840}{x} - 24 = 480 \Rightarrow 3x - \frac{3840}{x} = 24 \Rightarrow 3x^2 - 24x + 3840 = 0$$