

Exercise 12.2

1. Determine if the following are in proportion,

(a) 15, 45, 40, 120

(b) 33, 121, 9, 96

(c) 24, 28, 36, 48

(d) 32, 48, 70, 210

(e) 4, 6, 8, 12

(f) 33, 44, 75, 100

Ans. (a) 15 and 45 = $\frac{15}{45} = \frac{15 \div 15}{45 \div 15} = \frac{1}{3}$

40 and 120 = $\frac{40}{120} = \frac{40 \div 40}{120 \div 40} = \frac{1}{3}$

$\therefore 15 : 45 :: 40 : 120$

$\therefore 15, 45, 40,$ and 120 are in proportion.

(b) 33 and 121 = $\frac{33}{121} = \frac{33 \div 11}{121 \div 11} = \frac{3}{11}$

9 and 96 = $\frac{9}{96} = \frac{9 \div 3}{96 \div 3} = \frac{3}{32}$

Since $\frac{3}{11} \neq \frac{3}{32}$

$\therefore 33, 121, 9,$ and 96 are in proportion.

(c) 24 and 28 = $\frac{24}{28} = \frac{24 \div 4}{28 \div 4} = \frac{6}{7}$ 36 and 48 = $\frac{36}{48} = \frac{36 \div 12}{48 \div 12} = \frac{3}{4}$ Since $\frac{6}{7} \neq \frac{3}{4}$

$\therefore 24, 28, 36,$ and 48 are not in proportion.

(d) 32 and 48 = $\frac{32}{48} = \frac{32 \div 16}{48 \div 16} = \frac{2}{3}$ 70 and 210 = $\frac{70}{210} = \frac{70 \div 70}{210 \div 70} = \frac{1}{3}$ Since $\frac{2}{3} \neq \frac{1}{3}$

$\therefore 32, 48, 70,$ and 210 are not in proportion.

(e) 4 and 6 = $\frac{4}{6} = \frac{4 \div 2}{6 \div 2} = \frac{2}{3}$ 8 and 12 = $\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$

$\therefore 4 : 6 :: 8 : 12$

$\therefore 4, 6, 8,$ and 12 are in proportion.

(f) 33 and 44 = $\frac{33}{44} = \frac{33 \div 11}{44 \div 11} = \frac{3}{4}$ 75 and 100 = $\frac{75}{100} = \frac{75 \div 25}{100 \div 25} = \frac{3}{4}$

$$\therefore 33 : 44 :: 75 : 100$$

\therefore 33, 44, 75, and 100 are in proportion.

2. Write True (T) or False (F) against each of the following statements:

(a) $16 : 24 :: 20 : 30$

(b) $21 : 6 :: 35 : 10$

(c) $12 : 18 :: 28 : 12$

(d) $8 : 9 :: 24 : 27$

(e) $5.2 : 3.9 :: 3 : 4$

(f) $0.9 : 0.36 :: 10 : 4$

Ans. (a) $16 : 24 :: 20 : 30$

Product of the extreme terms = $16 \times 30 = 480$

Product of the middle terms = $24 \times 20 = 480$

\therefore The given statement (a) \rightarrow (T)

(b) $21 : 6 :: 35 : 10$

Product of the extreme terms = $21 \times 10 = 210$

Product of the middle terms = $6 \times 35 = 210$

\therefore The given statement (b) \rightarrow (T)

(c) $12 : 18 :: 28 : 12$

Product of the extreme terms = $12 \times 12 = 144$

Product of the middle terms = $18 \times 28 = 504$

Since $144 \neq 504$

\therefore The given statement (c) \rightarrow (F)

(d) $8 : 9 :: 24 : 27$

Product of the extreme terms = $8 \times 27 = 216$

The product of the middle terms = $9 \times 24 = 216$

The given statement (d) \rightarrow (T)

(e) $5.2 : 3.9 :: 3 : 4$

Product of the extreme terms = $5.2 \times 4 = 20.8$

Product of the middle terms = $3.9 \times 3 = 11.7$

Since $20.8 \neq 11.7$

The given statement (e) \rightarrow (F)

(f) $0.9 : 0.36 :: 10 : 4$

Product of the extreme terms = $0.9 \times 4 = 3.6$

Product of the middle terms = $0.36 \times 10 = 3.6$

\therefore The given statement (f) \rightarrow (T)

3. Are the following statements true?

(a) 40 persons : 200 persons = $\Pi 15 : \Pi 75$

(b) 7.5 litres : 15 litres = 5 kg : 10 kg

(c) 99 kg : 45 kg = $\Pi 44 : \Pi 20$

(d) 32 m : 64 m = 6 sec : 12 sec

(e) 45 km : 60 km = 12 hours : 15 hours

Ans. (a) 40 persons : 200 persons

$$= \frac{40}{200} = \frac{40 \div 40}{200 \div 40} = \frac{1}{5}$$

$$Rs\ 15 : 75 = \frac{15 \div 15}{75 \div 15} = \frac{1}{5}$$

\therefore Statement (a) is true.

(b) 7.5 liters: 15 liters

$$= \frac{7.5}{15} = \frac{75}{150} = \frac{75 \div 75}{150 \div 75} = \frac{1}{2}$$

$$5\ kg : 10\ kg = \frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$

\therefore Statement (b) is true.

$$(c)\ 99\ kg : 45\ kg = \frac{99}{45} = \frac{99 \div 9}{45 \div 9} = \frac{11}{5}$$

$$Rs\ 44 : 20 = \frac{44}{20} = \frac{44 \div 4}{20 \div 4} = \frac{11}{5}$$

\therefore Statement (c) is true.

$$(d)\ 32\ m : 64\ m = \frac{32}{64} = \frac{32 \div 32}{64 \div 32} = \frac{1}{2}$$

$$6\ sec\ sec : 12\ sec\ sec = \frac{6}{12} = \frac{6 \div 6}{12 \div 6} = \frac{1}{2}$$

\therefore Statement (d) is true.

$$(e)\ 45\ km : 60\ km = \frac{45}{60} = \frac{45 \div 15}{60 \div 15} = \frac{3}{4}$$

$$12\ hours : 15\ hours = \frac{12}{15} = \frac{12 \div 3}{15 \div 3} = \frac{4}{5}$$

Since $\frac{3}{4} \neq \frac{4}{5}$

∴ Statement (e) is not true.

4. Determine if the following ratios form a proportion. Also, write the middle terms and extreme terms where the ratios form a proportion.

(a) 25 cm : 1 m and ₹ 40 : ₹ 160

(b) 39 litres : 65 litres and 6 bottles : 10 bottles

(c) 2 kg : 80 kg and 25 g : 625 g

(d) 200 mL : 2.5 litres and ₹ 4 : ₹ 50

Ans. (a) 25 cm : 1 m = 25 cm : 100 cm [\because 1 m = 100 cm]

$$= \frac{25}{100} = \frac{25 \div 25}{100 \div 25} = \frac{1}{2}$$

$$\text{Rs. } 40 : \text{Rs } 160 = \frac{40}{160} = \frac{40 \div 40}{160 \div 40} = \frac{1}{4}$$

∴ The given ratios are in proportion.

Extreme terms are 25 cm and ₹160.

Middle terms are 1 m and ₹ 40.

$$\text{(b) } 39 \text{ litres} : 65 \text{ litres} = \frac{39}{65} = \frac{39 \div 13}{65 \div 13} = \frac{3}{5}$$

$$6 \text{ bottles} : 10 \text{ bottles} = \frac{6}{10} = \frac{6 \div 2}{10 \div 2} = \frac{3}{5}$$

∴ The given ratios are in proportion.

Extreme terms are 39 liters and 10 bottles.

Middle terms are 65 liters and 6 bottles.

$$\text{(c) } 2 \text{ kg} : 80 \text{ kg} = \frac{2}{80} = \frac{2 \div 2}{80 \div 2} = \frac{1}{40}$$

$$25 \text{ g} : 625 \text{ g} = \frac{25}{625} = \frac{25 \div 25}{625 \div 25} = \frac{1}{25}$$

$$\text{Since } \frac{1}{40} \neq \frac{1}{25}$$

∴ The given ratios are not in proportion.

(d) 200 mL : 2.5 litres = 2.5 litres = 2.5 x 1000 mL = 2500 mL

$$200 \text{ mL} : 2500 \text{ mL} = \frac{200 \div 100}{2500 \div 100} = \frac{2}{25}$$

$$\text{Rs. } 4 : 50 = \frac{4}{50} = \frac{4 \div 2}{50 \div 2} = \frac{2}{25}$$

$$\text{Since } \frac{2}{25} = \frac{2}{25}$$

∴ The given ratios are in proportion.

Extreme terms are 200 mL and ₹ 50

Middle terms are 2.5 liters and ₹ 4.